

# **1-GHz and 2.8-GHz CMOS Injection-locked Ring Oscillator Prescalers**

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# Outline

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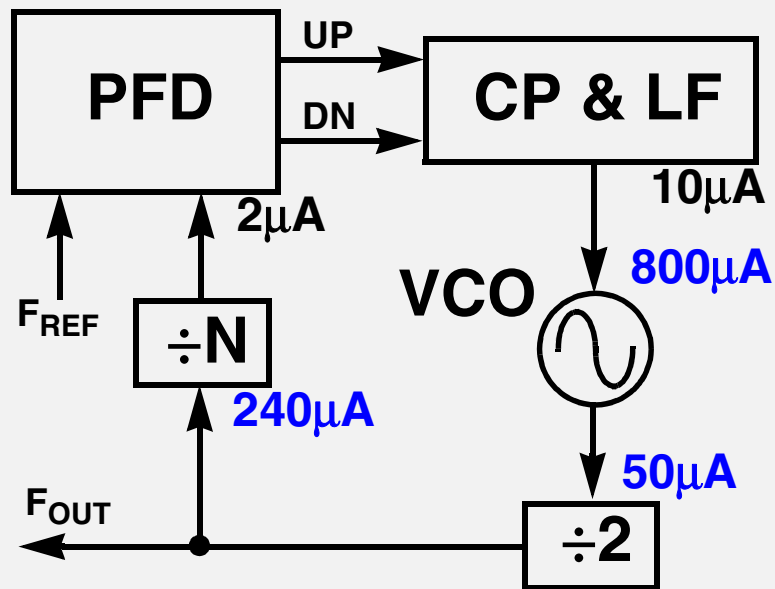
- ***Introduction***
- Injection Locking Theory
- Circuit Implementation
- Measured Results
- Conclusion

## Goals

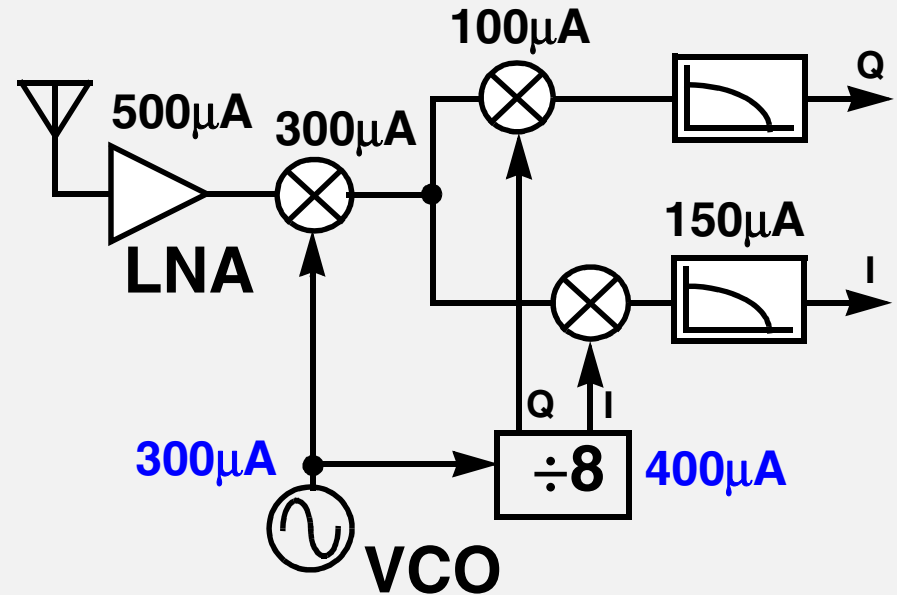
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- . Understand the Injection-locking mechanism**
- . Grasp the limitations of Injection-locked Frequency Dividers**
- . Design Injection-locked Frequency Divider using a Ring Oscillator**

# Motivation: Low-power Frequency Synthesis



320 MHz CMOS PLL  
[V.Kaenel'96]



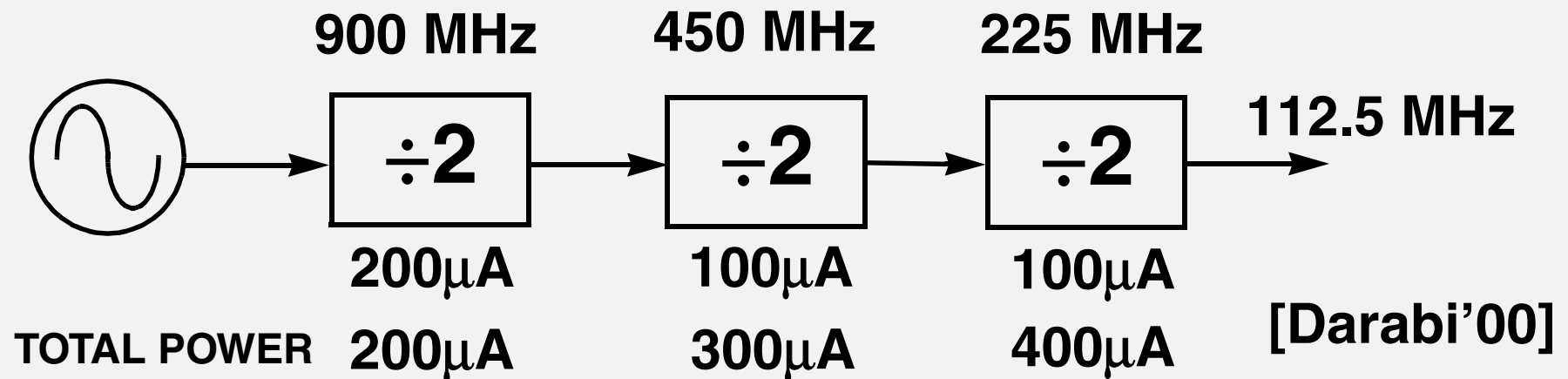
900 MHz CMOS RECEIVER  
[Darabi'00]

- Frequency synthesizers are implemented using PLLs.
- Major sources of power dissipation are the VCO and Frequency Divider.

## Frequency Divider Power Trade-off

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### POWER INCREASES WITH DIVISION RATIO



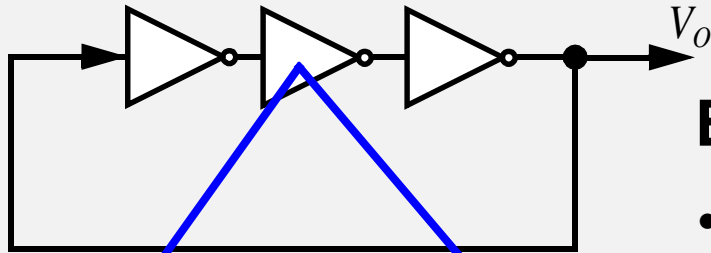
- We propose a technique in which power **decreases** with division ratio.

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# Ring Oscillator Model



## BARKHAUSEN CRITERIA

- Necessary conditions for oscillation

### GAIN CONDITION

$$|H(j\omega_o)| \geq 1$$

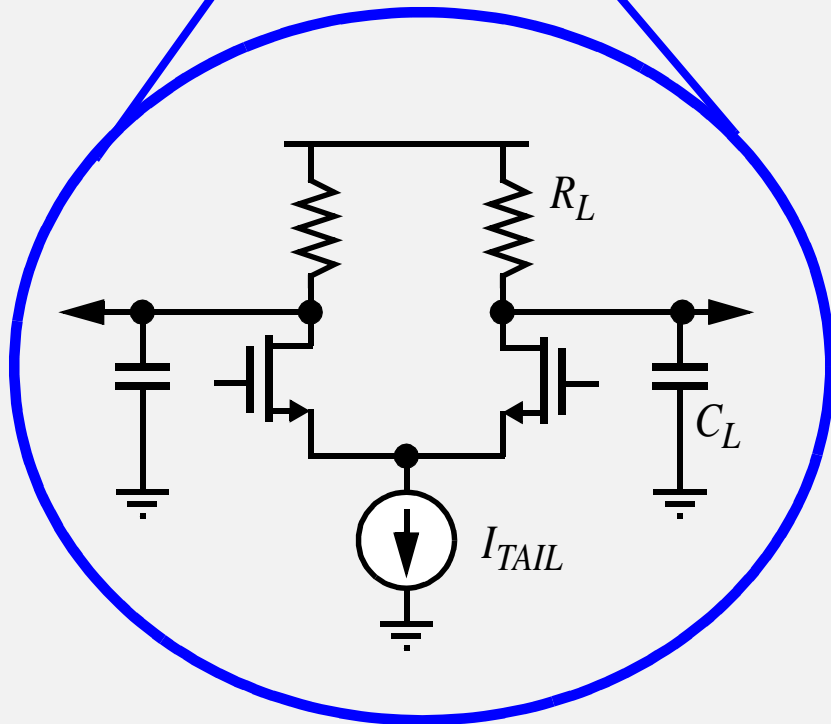
### PHASE CONDITION

$$\angle H(j\omega_o) = 180^\circ$$

### SMALL-SIGNAL MODEL

$$H_S(j\omega) = \frac{H_O}{1 + j\omega/\omega_P}$$

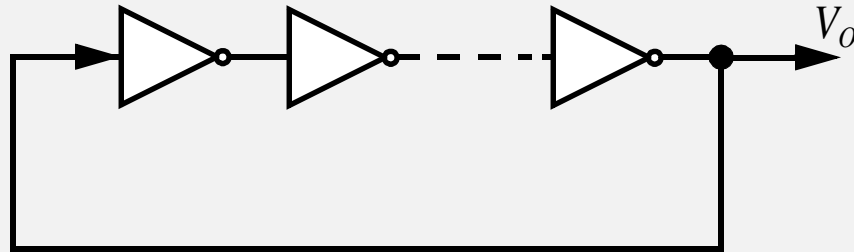
$$\omega_P = \frac{1}{R_L C_L}$$



- Neglect feedforward zero

## Ring Oscillator Model (II)

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### GAIN CONDITION

$$H_O \geq \sqrt{1 + \tan^2\left(\frac{\pi}{n}\right)}$$

### PHASE CONDITION

$$\omega_P = \frac{\omega_0}{\tan\left(\frac{\pi}{n}\right)}$$

### N-STAGE MODEL

$$H(j\omega) = \frac{H_O^n}{\left(1 + j\frac{\omega}{\omega_0} \tan\left(\frac{\pi}{n}\right)\right)^n}$$

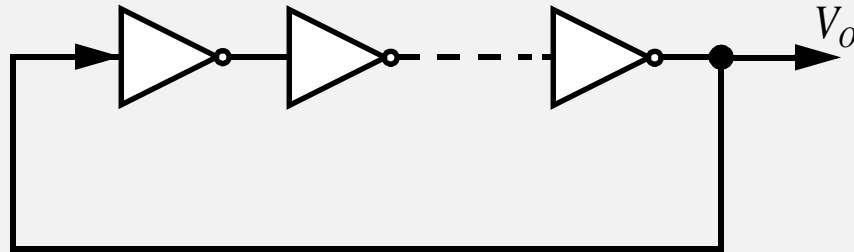
$$n > 2$$

- $\omega_0$  is free-running oscillator frequency.
- Each stage contributes  $\pi/n$  to the phase.



## Ring Oscillator Model (III)

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### EXAMPLE

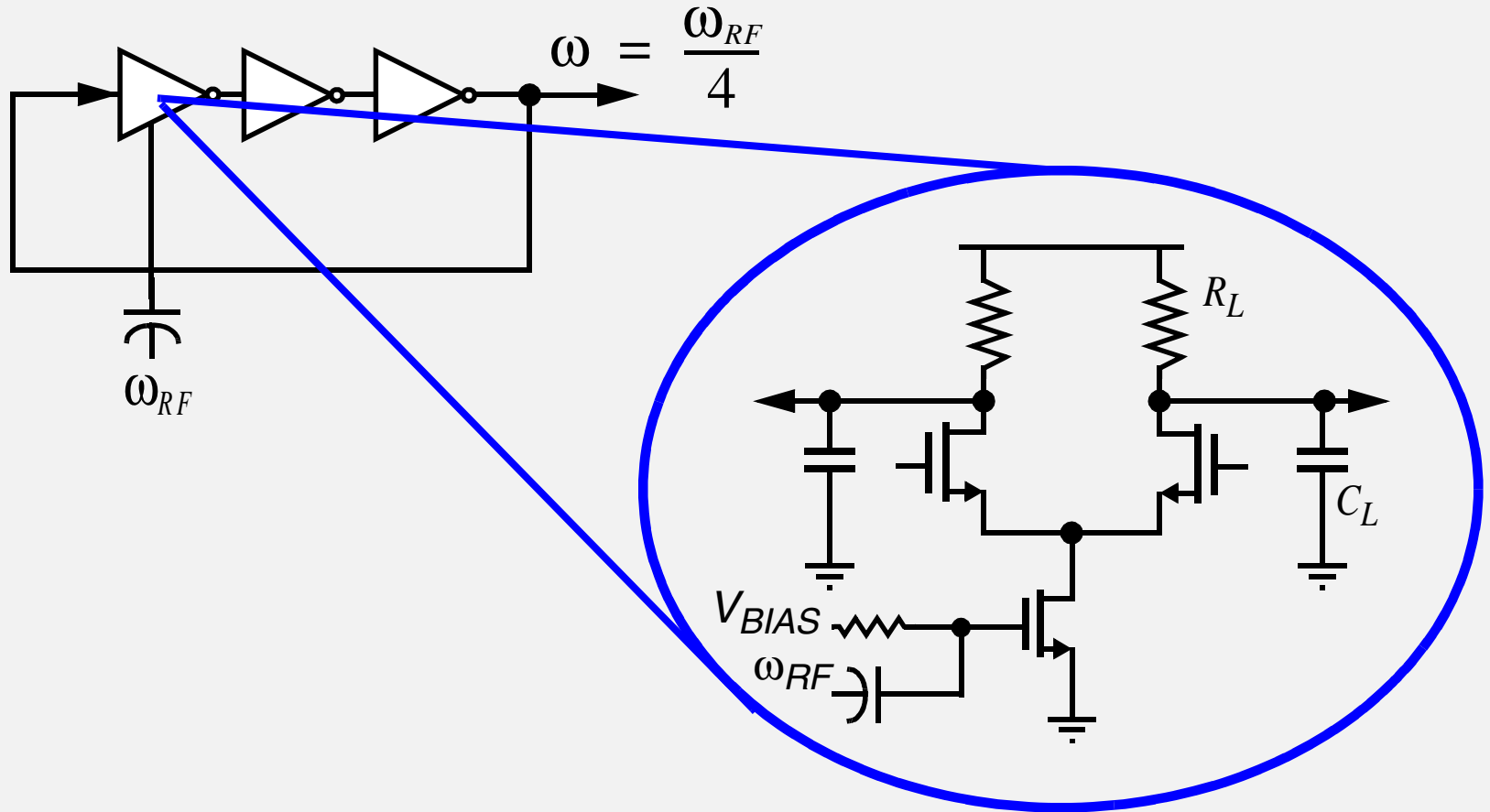
$$H(j\omega) = \frac{H_0^n}{\left(1 + j\frac{\omega}{\omega_0} \tan\left(\frac{\pi}{n}\right)\right)^n}$$

$n$	$H_0$	$\omega_p$
3	2.00	$0.58 \omega_0$
4	1.41	$\omega_0$
5	1.24	$1.38 \omega_0$

- DC gain  $H_0$  decreases with number of stages.
- Poles  $\omega_p$  coincide with  $\omega_0$  only for  $n=4$ .

# Injection-locked Ring Oscillator

## EXAMPLE: 3-stage, Divide by 4

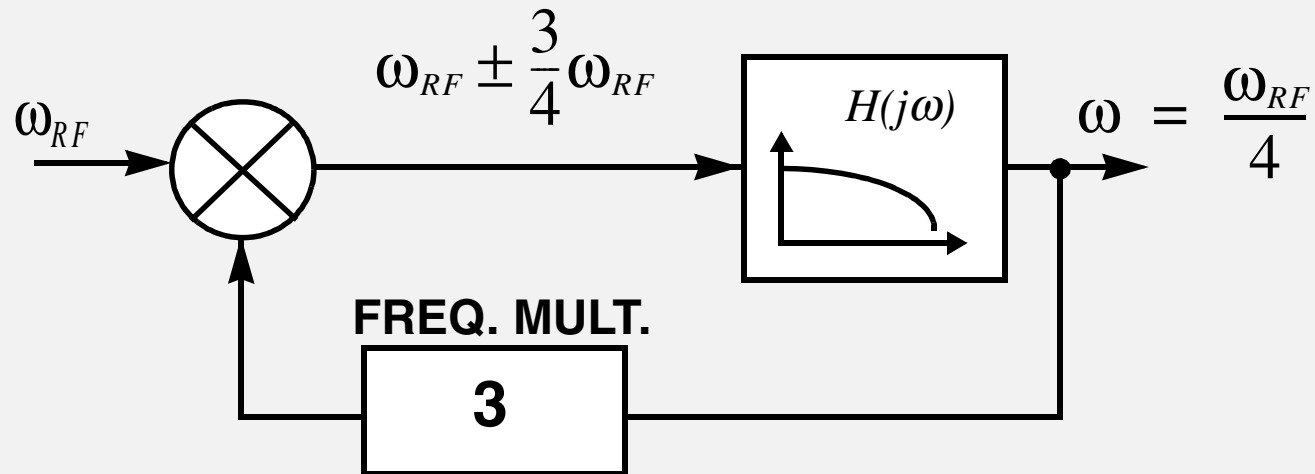


- An oscillator can be injection-locked to a harmonic of the free-running oscillation frequency.

# Regenerative Divider [Miller 1939]

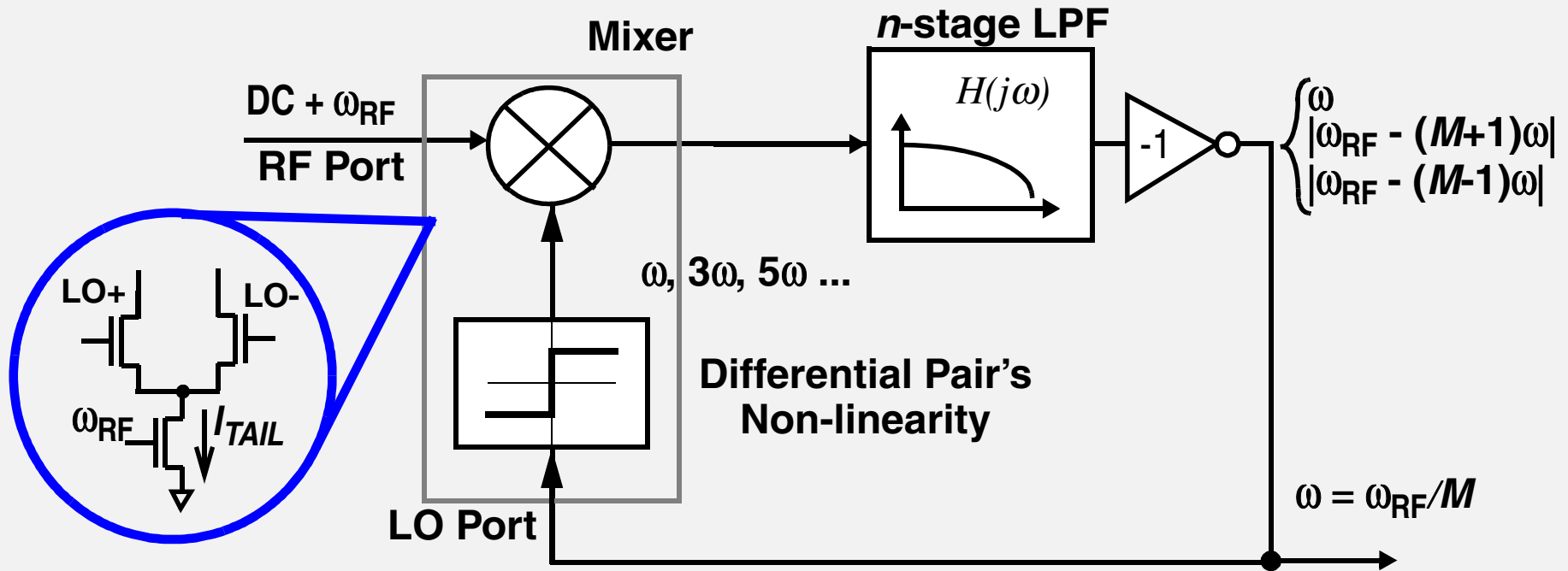
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## EXAMPLE: Divide by 4



- Commonly used where the frequency of operation is very high, beyond what can be achieved with flip-flop based circuits.
- Frequency multiplier can represent non-linearities present in the circuit.
- Used a model similar to Miller's, since the locking mechanisms are identical.

# Model for Injection-locked Frequency Divider



## MIXER

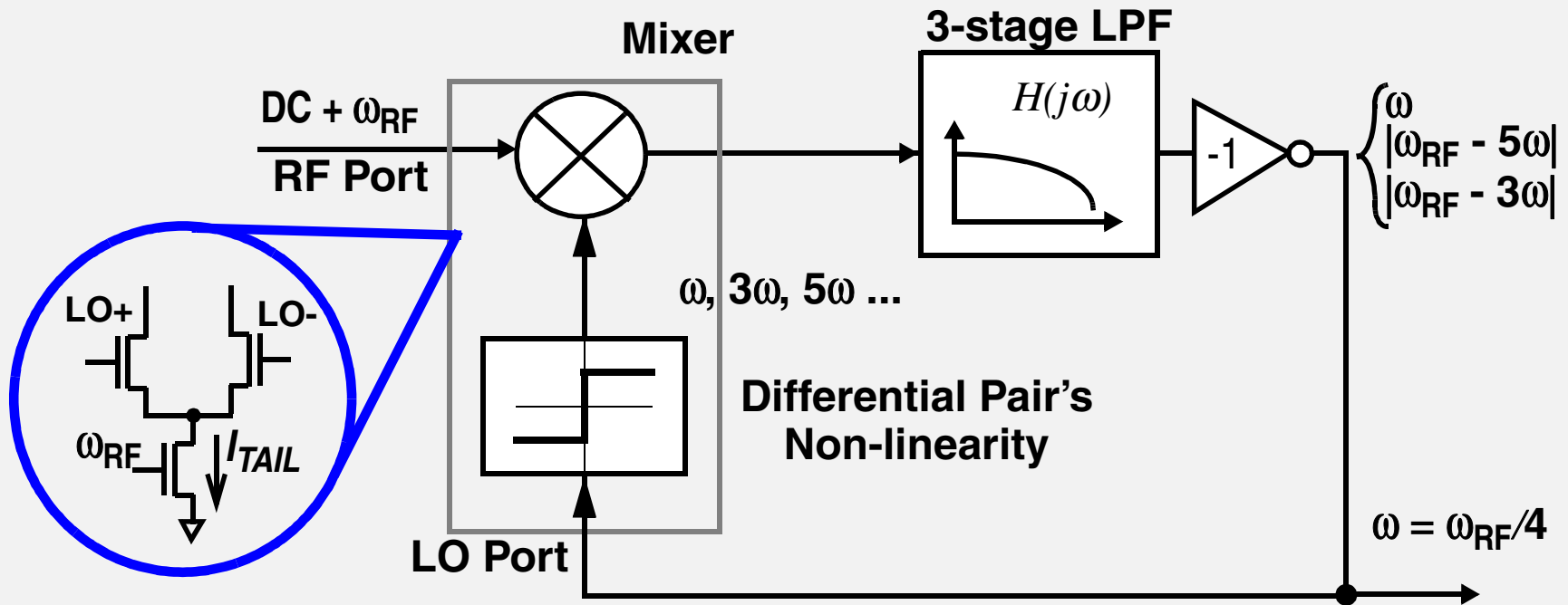
- Differential-pair single-balanced mixer
- Injected  $\omega_{RF}$  into the tail device

## FILTER

- Suppress products  $> \omega$
- $V_O$  is sinusoidal (small  $n$ ).

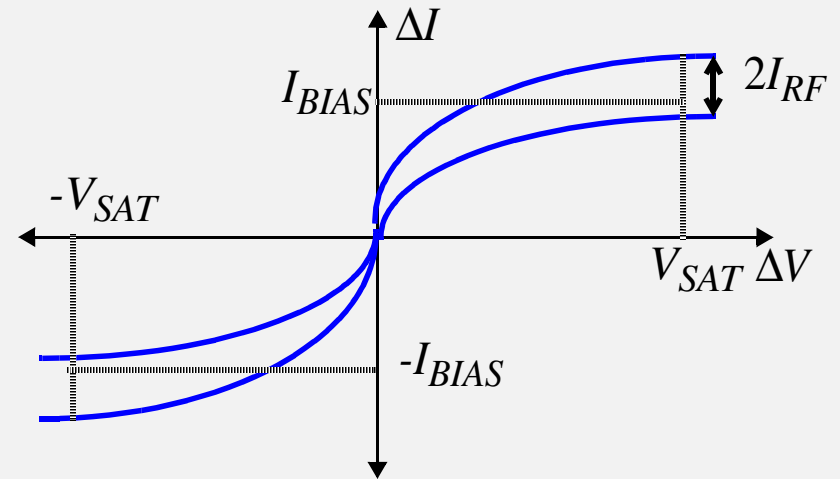
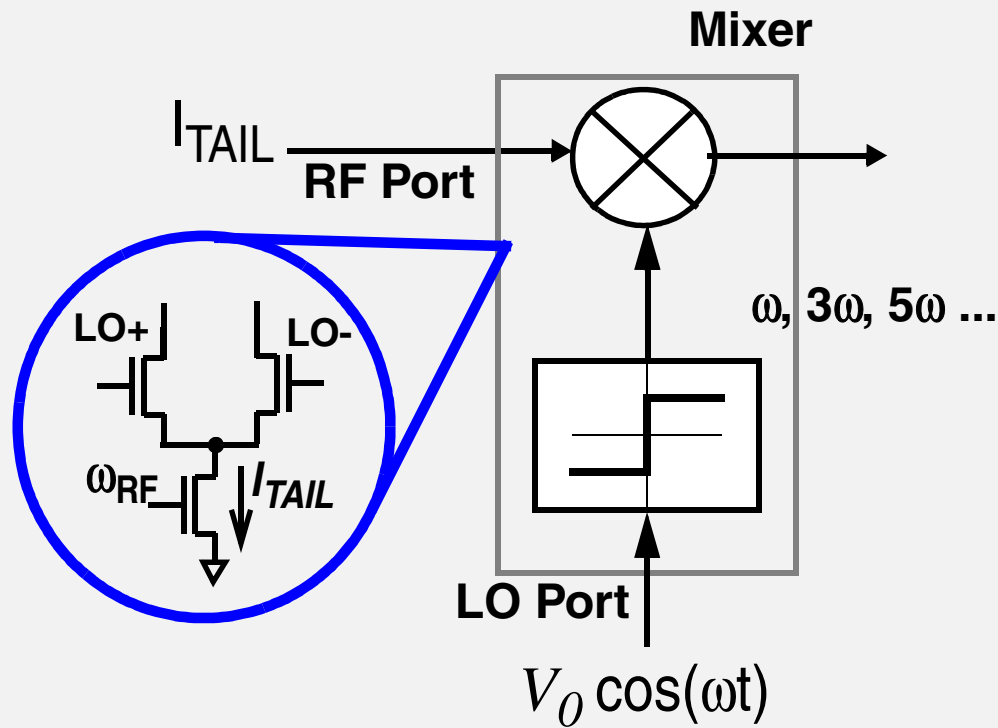
# Model for Injection-locked Frequency Divider (II)

## EXAMPLE: 3-stage, Divide by 4



- With no injection,  $\omega = \omega_0$ .

# Mixer



$$I_{TAIL} = I_{RF} \cos(\omega_{RF}t + \alpha) + I_{BIAS}$$

$$V_{SAT} = \sqrt{\frac{(W/L)_{TAIL}}{(W/L)_{DIFF}}} \cdot V_{ODT}$$

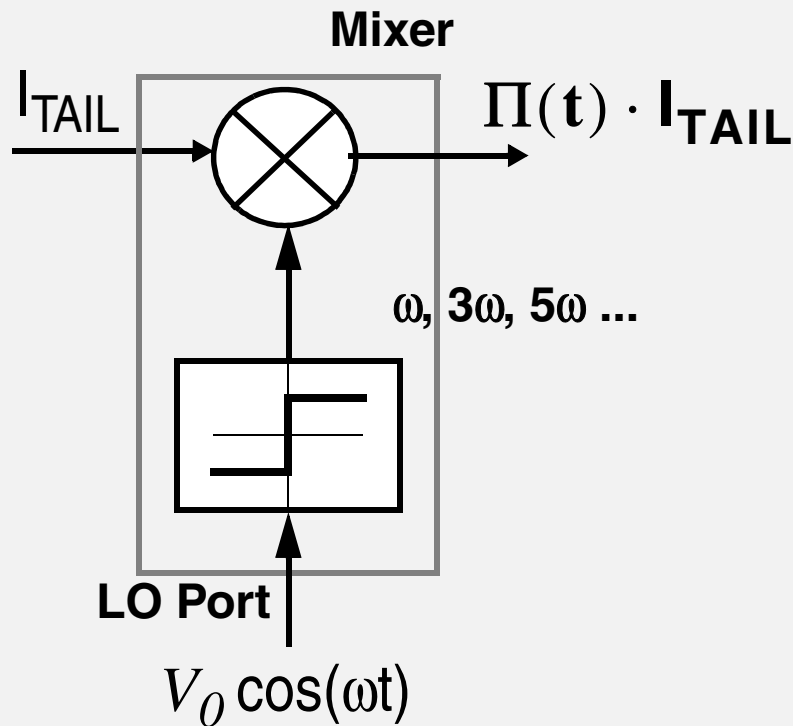
- The differential-pair is non-linear with odd symmetry.
- Non-linearity produces odd harmonics at  $3\omega$ ,  $5\omega$ , etc.
- $I_{TAIL}$  is modulated by  $\omega$  and its harmonics.

## Mixer (II)

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### DEFINE SWING RATIO

$$\rho_s = V_0 / V_{SAT} \gg 1 \text{ (Square Wave)}$$



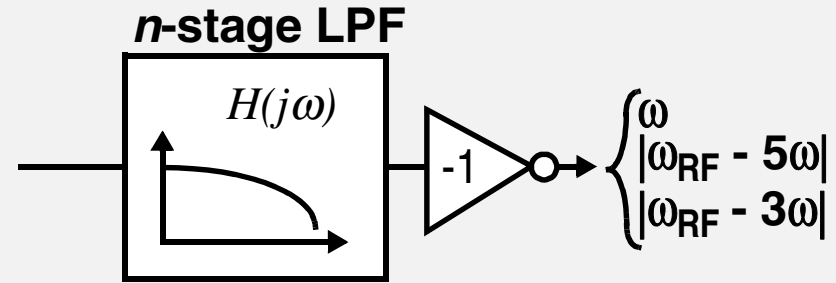
### Fourier Coefficients of Mixing Function $\Pi(t)$

$$C_k = \begin{cases} \frac{1}{k\pi} \cdot (-1)^{(k-1)/2} & \text{odd } k \\ 0 & \text{otherwise} \end{cases}$$

# Filter

## Use Ring Oscillator Model

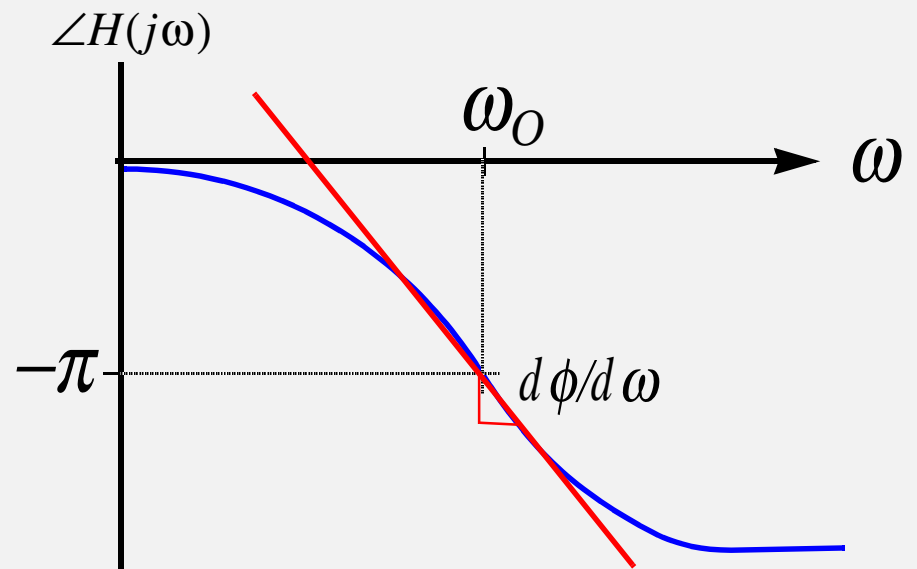
$$H(j\omega) = \frac{H_0^n}{\left(1 + j\frac{\omega}{\omega_0} \tan\left(\frac{\pi}{n}\right)\right)^n}$$



## Linearize Phase of $H(j\omega)$

$$-\angle H(j\omega) \cong \pi + \frac{n \sin\left(\frac{2\pi}{n}\right)}{2} \cdot \frac{\Delta\omega}{\omega_0}$$

$$\Delta\omega = \omega - \omega_0$$





# Describing Function Analysis

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## WRITE PHASE EXPRESSION AROUND THE LOOP

$$\underbrace{\operatorname{atan}\left(\frac{\eta_i(C_{M-1} - C_{M+1})\sin\alpha}{C_1 + \eta_i(C_{M-1} + C_{M+1})\cos\alpha}\right)}_{\text{MIXER}} = \underbrace{-\angle Hj\omega - \pi}_{\text{FILTER}} \quad \eta_i = \frac{I_{RF}}{2I_{BIAS}} \quad \text{INJECTION EFFICIENCY}$$

**FIND SOLUTION FOR  $\alpha \in (-\pi, \pi]$ .**

- If  $V_O$  is large, then the injection locking dynamics are determined by the phase relationship around the loop (phase-limited) and therefore we can ignore the amplitude expression.

# Locking Range of Injection-locked Ring Oscillator

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$$LR \cong \frac{4}{n \sin\left(\frac{2\pi}{n}\right)} \operatorname{atan}\left(\frac{k_0}{\sqrt{1 - k_1^2}}\right)$$

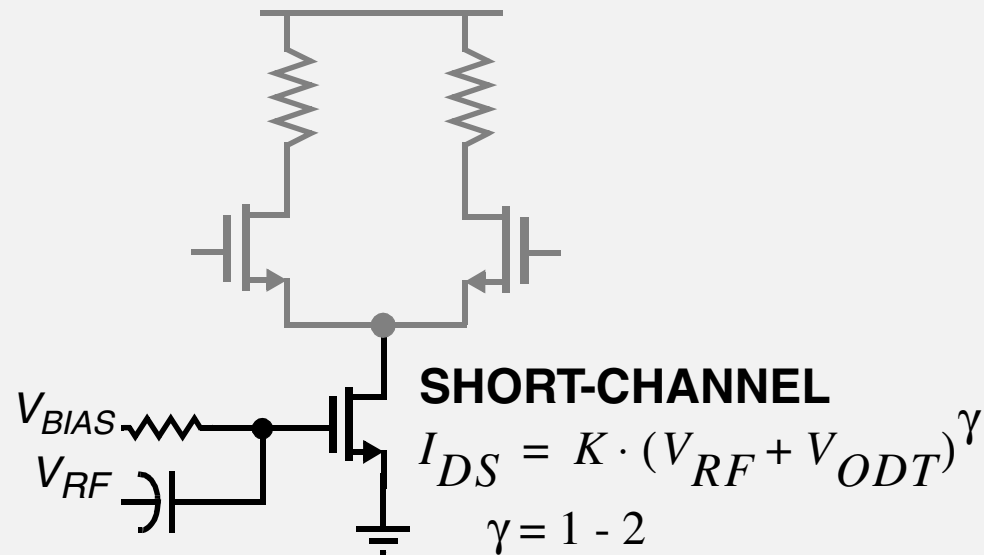
**WHERE**

$$k_0 = \eta_i \left| \frac{C_{M-1} - C_{M+1}}{C_1} \right| \quad k_1 = \eta_i \left| \frac{C_{M-1} + C_{M+1}}{C_1} \right|$$

- Function of injection efficiency  $\eta_i$ , and the magnitude of the Fourier coefficients  $C_{M-1}$  and  $C_{M+1}$ .
- For small values of injected signal the locking range increases linearly with the injected signal strength.

# Limited Injection Efficiency and Parasitics

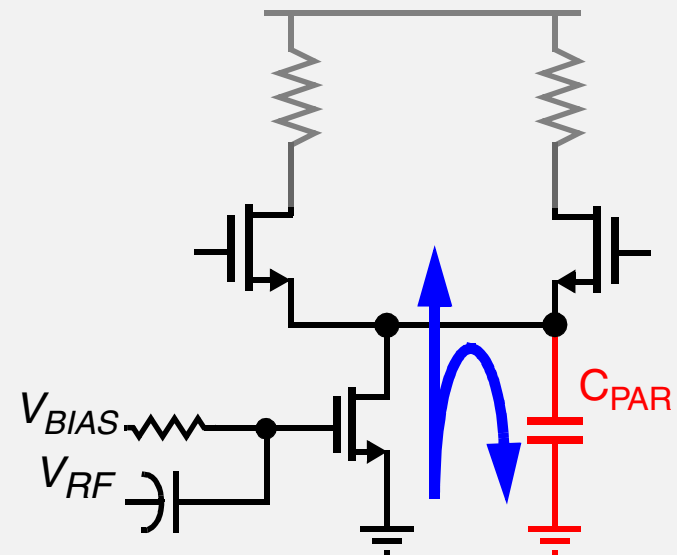
## INJECTOR NON-IDEALITIES



$$\eta_i = \frac{V_{RF}}{2V_{ODT}} \cdot \gamma$$

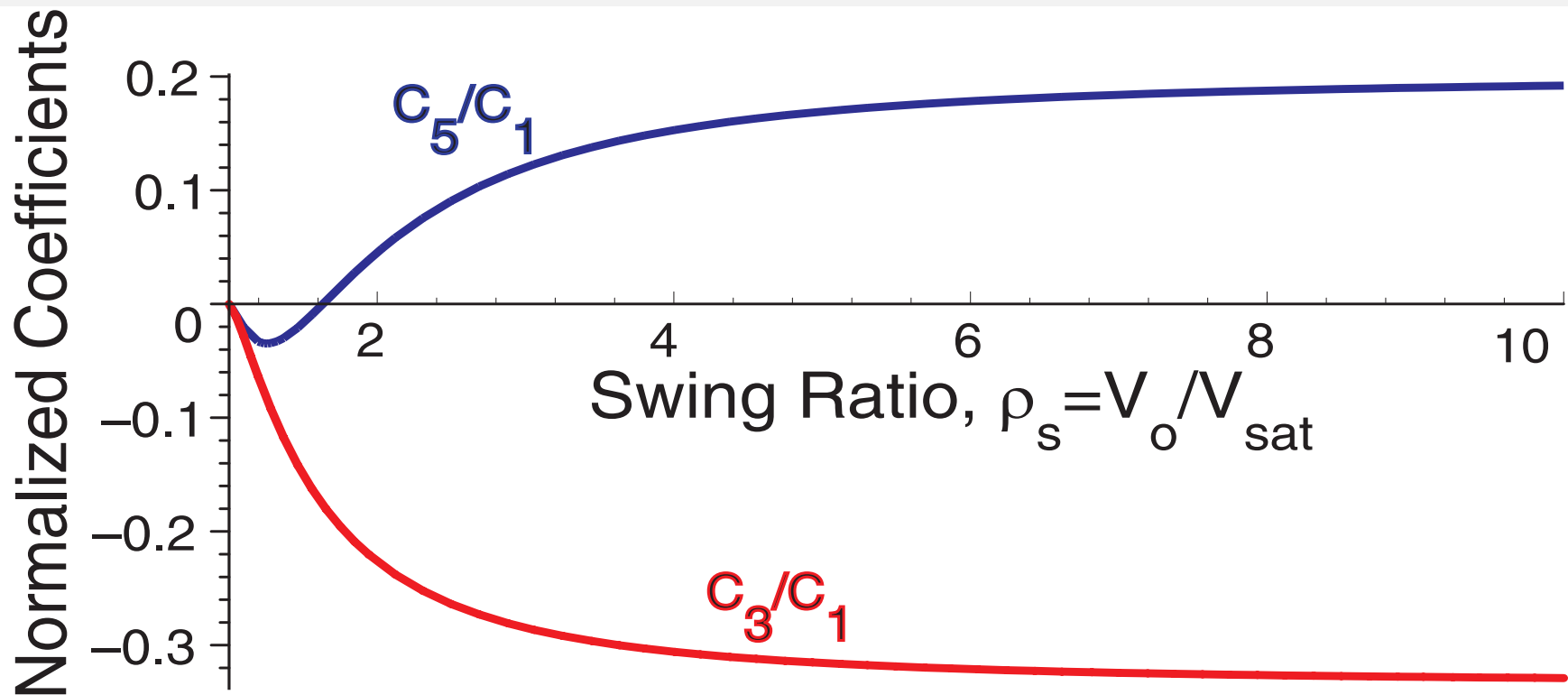
- Limited injection efficiency due to short-channel effects and tail device non-linearity.

## TAIL PARASITICS



- Shunt path for  $I_{RF}$  reducing the injection efficiency at high frequencies.

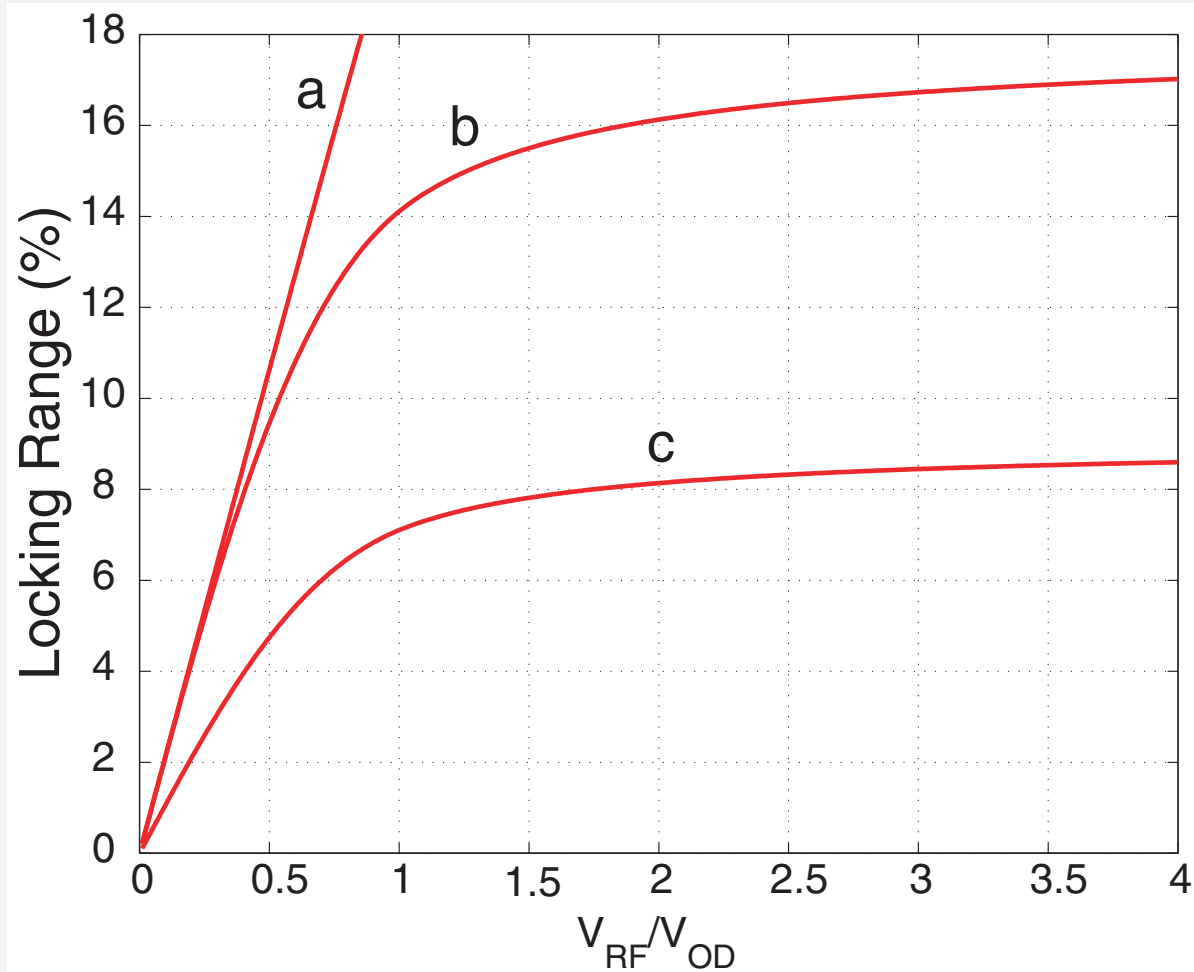
## Limited Mixer Gain



- The assumption that the mixer's switching function is a square wave is very accurate if the swing ratio  $\rho_s \gg 1$ .
- As  $\rho_s$  gets smaller, the normalized coefficients  $C_k/C_1$  are significantly smaller, thus degrading the locking range.

## Example: 5-stage, Modulo-8 Ring Oscillator

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(a) Ideal (phase-limited) case

(b) Compression due to Injector non-linearity (square-law device)

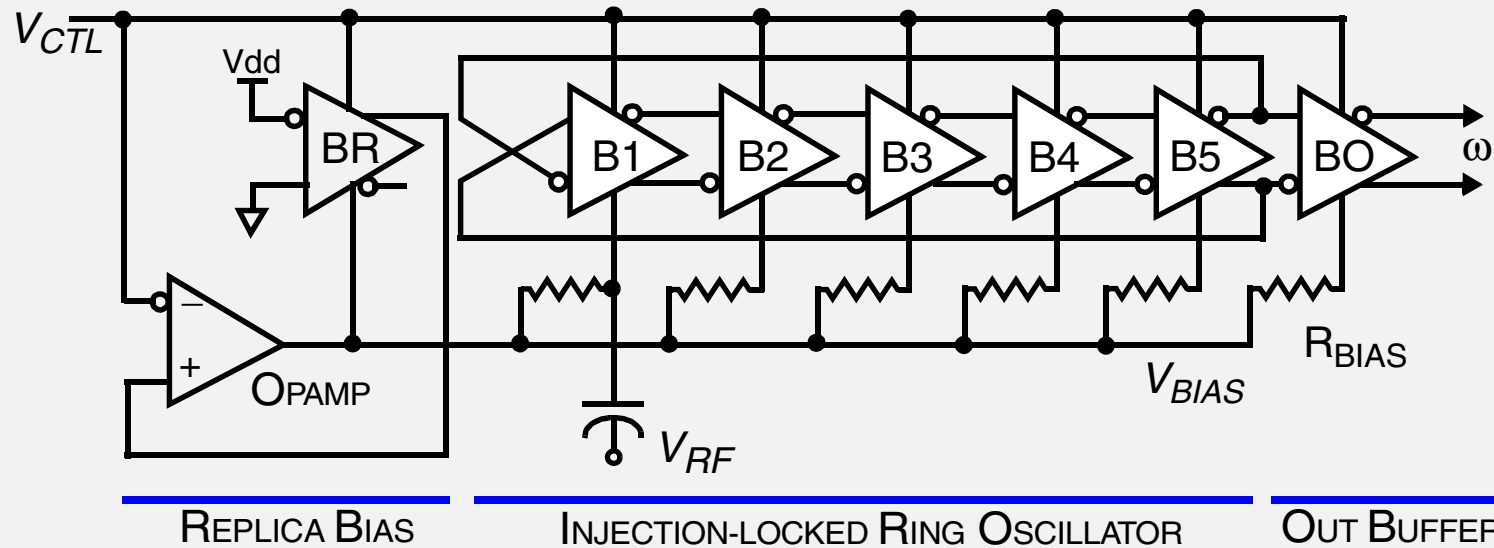
(c) Effects of Injector non-linearity and tail parasitics (50% loss)

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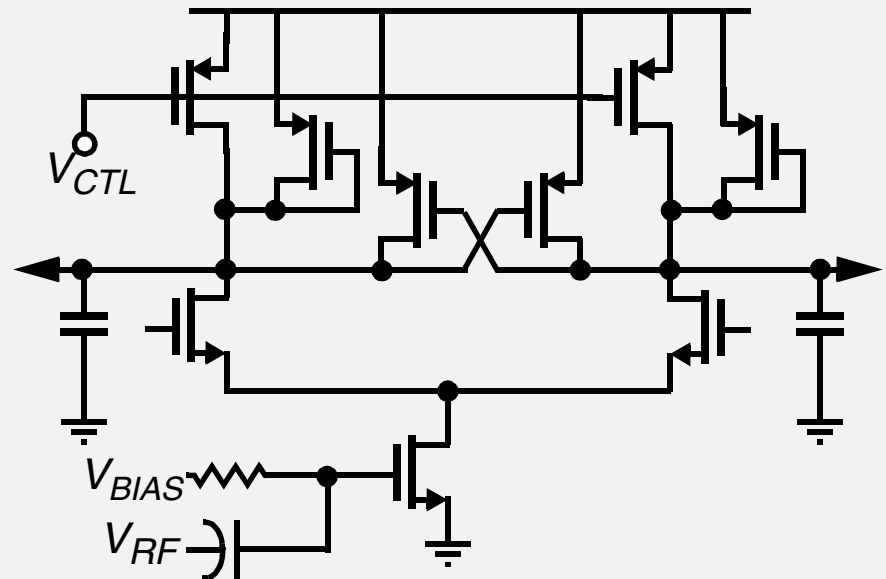
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# 5-stage Injection-locked Ring Oscillator Frequency Divider

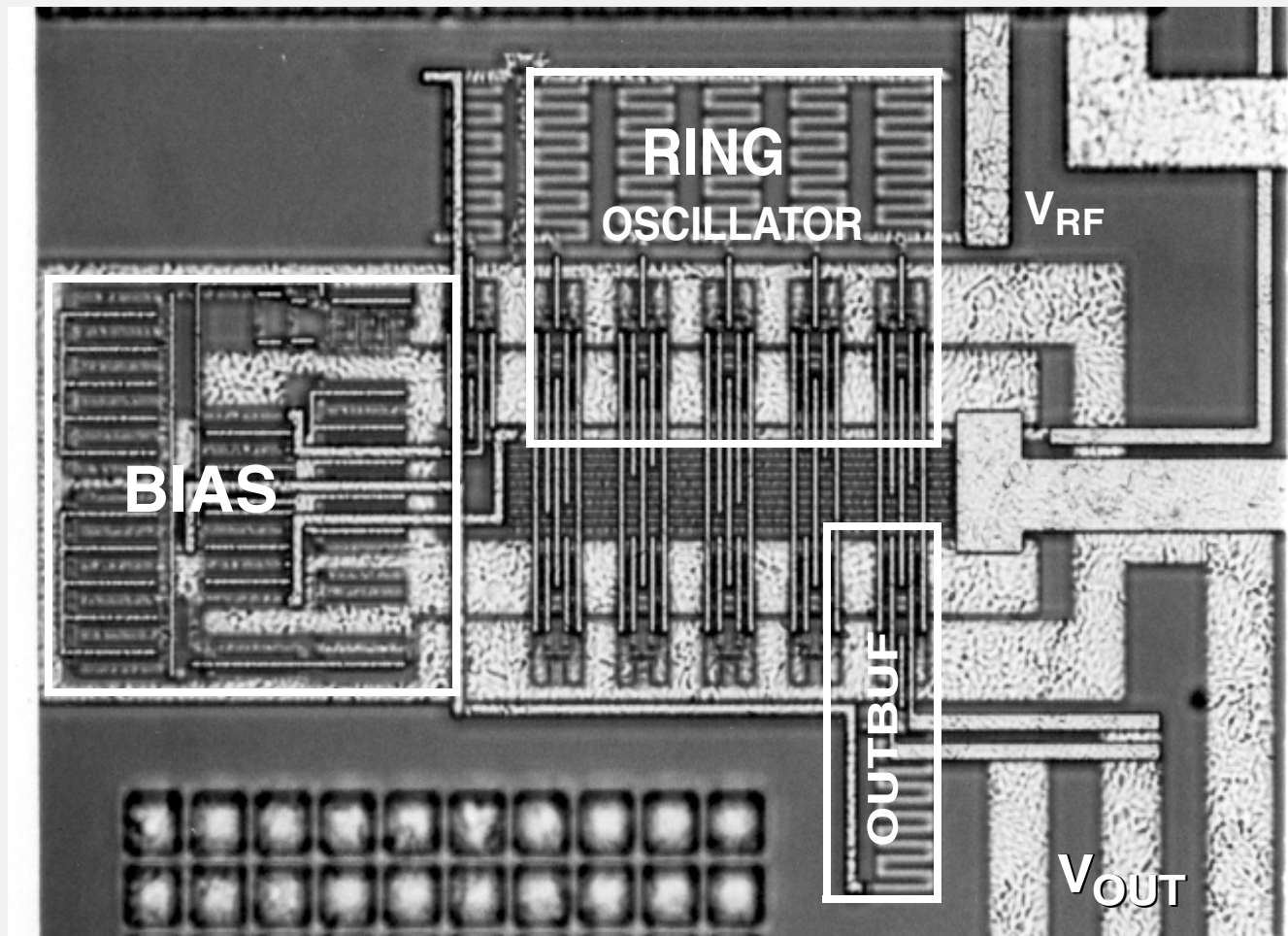


- Used modified cross-coupled symmetric load buffers.
- RF signal injected at the tail of the first buffer (single-balanced mixer).
- The buffer stages behave as the  $H(j\omega)$  filter.



# Die Micrograph: 5-stage Ring Oscillator Divider

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- Fabricated 3 and 5-stage ring oscillators.
- 0.24- $\mu\text{m}$  CMOS
- 0.012 mm<sup>2</sup> of area



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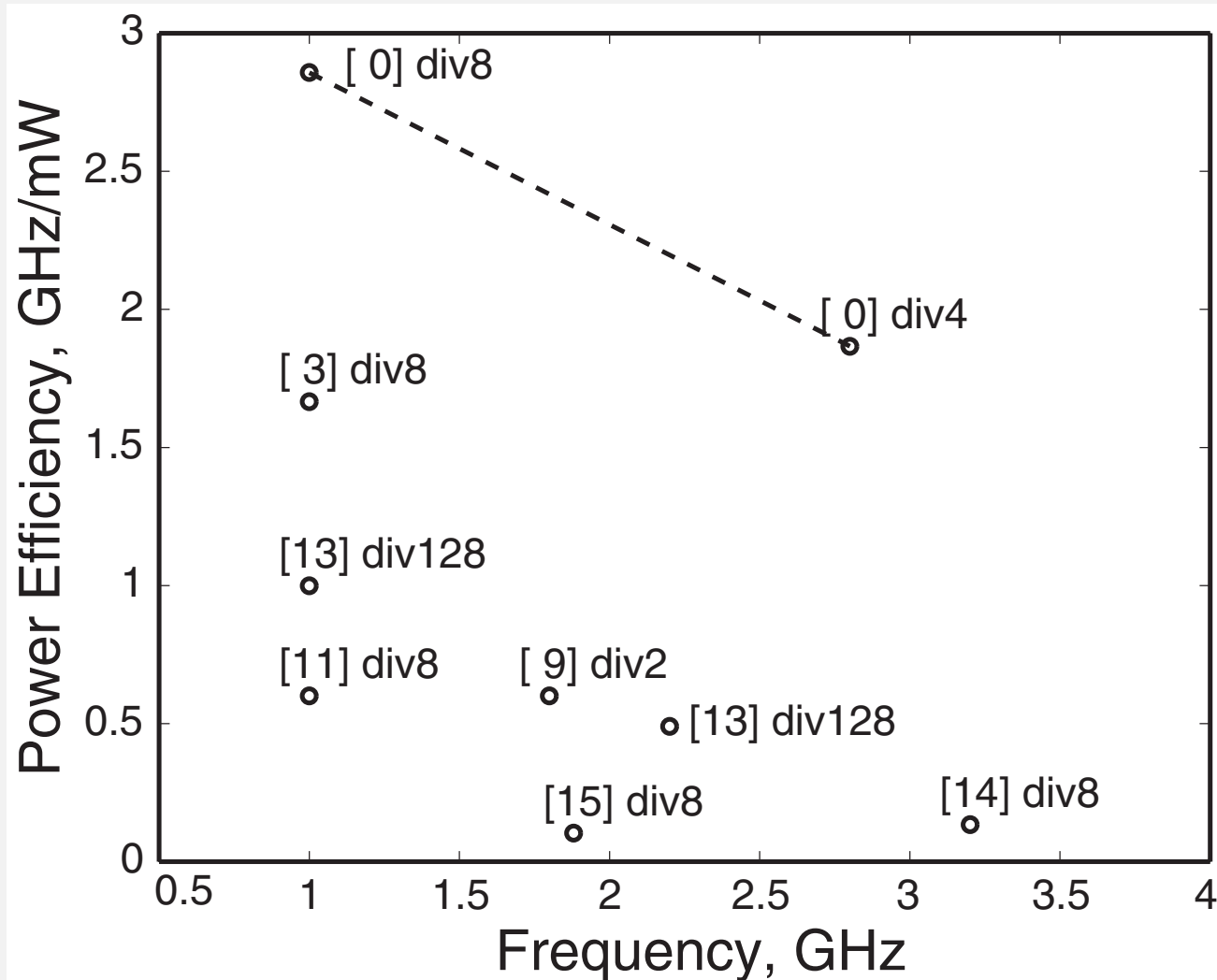
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## Results

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	<b><i>5-stage ILFD</i></b>	<b><i>3-stage ILFD</i></b>
Injected Frequency	1.0 GHz	2.8 GHz
Free-running Frequency	125 MHz	700 MHz
Phase Noise @ 100KHz	-110 dBc/Hz	-106 dBc/Hz
<b><i>Input Locking Range</i></b>		
Modulo-2	12.7 MHz (-3dBm)	125 MHz (-3dBm)
Modulo-4	32 MHz (-3dBm)	56 MHz (-5dBm)
Modulo-6	17 MHz (-3dBm)	no-lock
Modulo-8	20 MHz (-3dBm)	no-lock
<b><i>Power dissipation</i></b>		
Vdd	1.5 V	3.0 V
I <sub>core</sub>	233 $\mu$ A	331 $\mu$ A
I <sub>bias</sub>	108 $\mu$ A	661 $\mu$ A
Core power	350 $\mu$ W	993 $\mu$ W
Power efficiency	2.86 GHz/mW	2.82 GHz/mW

# Power Efficiency of Injection-locked Ring Oscillator



- [0] 5-stage (div-8) = 2.86 GHz/mW @ 1GHz
- [0] 3-stage (div-4) = 2.82 GHz/mW @ 2.8GHz

## What We Learned

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### LOCKING RANGE COMPARISON

	5-stage (div-8) @ 1 GHz	3-stage (div-4) @ 2.8 GHz
THEORY	9%	34%
SIMULATION	5%	17%
TEST	2%	2%

- Large tail device ( $W/L=10.2/1$ ) caused loss of  $I_{RF}$ . Need to lower tail node parasitics to increase the injection efficiency.
  - Resonating tail with an inductor [*Wu, ISSCC'01*] is not practical at sub-GHz frequencies.
- Small swing ratio ( $\rho_s \approx 3-4$ ) caused reduction in mixer gain. Need to increase output swing and reduce  $V_{SAT}$ .

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## Conclusion

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- Described the injection locking mechanism and how it applies to CMOS ring oscillators.
- Showed the design of frequency dividers that can operate up to 2.8-GHz by exploiting injection locking in differential CMOS ring oscillators.
- Showed measured results for 1-GHz and 2.8-GHz injection-locked frequency dividers fabricated in a 0.24- $\mu\text{m}$  CMOS technology.

# Acknowledgments

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**National Semiconductor**